

Reversibility

Exploring what makes something reversible

Learning Goals

- Understand what it means to be able to reverse an action or a mathematical operation.
- Explain why particular actions or mathematical operations are reversible or irreversible.



Materials

- Reversibility with Paper* sheets
- Reversibility Cards (1 set)
- Sticky notes or index cards
- Chart paper (optional)
- Reversible or Not?* worksheet (optional)
- Is it Reversible?* worksheet



Background Knowledge

This activity conveys the idea of reversibility, or “uncomputing” in quantum computing. The basic idea of reversibility is something children can grasp – zipping a zipper is reversible, yet cracking an egg is not. Because of the laws of quantum physics, all quantum computation must be reversible. An operation is reversible if you can perform an opposite operation and get back to where you started. The jump to mathematical operations, only appropriate for older audiences, brings this concept closer to quantum computing. When a classical computer performs the operation: $12 + 7 = 19$, some information is lost. With only the result and operation (addition), we cannot get back to the inputs of 12 and 7 since many pairs of numbers sum to 19. However, if we keep one of the inputs (for example, $12 + 7 = 19$ (via 7)) then we can get back the 12 by subtracting 7 from 19. Quantum computing requires more memory bits because it has to maintain extra information in order to satisfy the reversibility constraint.

Importance in Quantum

Computing

This activity introduces participants to the concept of reversibility, which is a key theme in quantum computing. Because of quantum physics, all quantum computations must be reversible.

Preparation

- Make copies of the *Reversibility with Paper* sheet and cut along the dotted lines.
- Identify a location (e.g., wall space, chart paper) to post items generated by participants.
- Choose the version of *Is it Reversible?* that best fits your audience and make copies.

Facilitating the Activity

ENGAGE



Literacy
Connection

1. Choose one of the following options to begin.
 - a. Consider reading or having available one or more of the following:
 - *Bears in the Night* by Stan and Jan Berenstain
 - *Go Away, Big Green Monster!* by Ed Emberly
 - *We're Going on a Bear Hunt* by Michael Rosen and Helen Osenbury

In these stories, the characters end up in the same place they began. When discussing the story with participants, introduce the idea of reversing actions by comparing it to doing something backwards. For example, you can build a stack of blocks, then take them down one by one.

- b. Ask: *What do you think it means for something to be reversible? Is jumping in a puddle reversible?* You want to elicit more than just jumping out of the puddle because there are many potential elements to think about when we think about if something is reversible. Ask follow-up questions such as:
 - What do you need to do to reverse it?
 - Do you need to dry off your clothes?
 - If your clothes are stained, is that reversible?
 - Is the puddle the same?

ACTIVITY



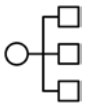
Quantum
Connection

1. Introduce the purpose of this activity. Tell participants that one thing that computers do is perform a lot of mathematical operations. Quantum computing is a new type of computation. It has the potential to perform some types of calculations much faster than current computers. However, it has a limitation – all quantum operations must be reversible. If something is reversible, it means you can get back to what you started with. Let's explore what reversibility means in everyday actions.
2. Give each participant one of the prepared *Reversibility with Paper* sheets. Ask them to perform the action described on the sheet. Then ask them to reverse the action. Facilitate a discussion about reversibility by asking questions such as:
 - a. Were you able to reverse your action? How?
 - b. Can you get the paper back to the way it was when I gave it to you?
 - c. Can you reverse your action so that no one can tell what happened to the paper?

Reversibility Cards

In this discussion, you want to clarify the difference between fixing something (e.g., taping the paper back together, unfolding the paper airplane) and reversing back to the original state.

3. Show participants the Reversibility Cards. Ask participants to determine whether they think the action or change represented in the images on a given card is reversible, meaning they can be undone or reversed. Sort the cards into “reversible” and “irreversible” actions/changes. When a participant determines whether an action/change is reversible or not, probe for the explanation or reasoning behind their answer. As needed, return to the distinction between fixing something and reversing a change. Note that participants are likely to vary in the degree to which they think small differences that remain after reversing are important.



Differentiation Note: For younger participants, show the cards one at a time and consider the order in which you present them, starting with less ambiguous cards first.

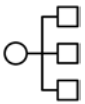
DISCUSSION

1. Facilitate a discussion about determining if an action/change is reversible. Ask questions such as:
 - How did you decide if something was reversible or not?
 - Which card was easy to categorize? Why?
 - Which card was the most difficult to categorize? Why?
 - Of all the reversible actions, which is the most difficult to reverse? Which is the easiest? Why?
 - Did you find any actions that you thought could be both reversible and irreversible? How did you decide?
2. Lead participants in brainstorming other reversible and irreversible actions or changes. Ask them to write each idea on a sticky note or index card, including their reasoning of why it is reversible or irreversible. Alternatively, ask participants to complete the *Reversible or Not?* worksheet and provide time for them to ask another participant to share their thoughts on the action or change. Show participants where to post their ideas on the Reversible Actions/Changes and Irreversible Actions/Changes charts.
3. Facilitate a discussion about what attributes you look for to determine if an action/change is reversible. Ask questions such as:
 - What rules or reasoning did you use to decide whether something was reversible or not?
 - Do all reversible actions have anything in common? What about irreversible actions?

Reversibility Cards

Document their ideas on a Reversibility Rules chart.

4. Ask participants to complete the *Is It Reversible?* worksheet.
5. Tell participants that while quantum computers are fast at some things, they can only do so much because everything they do must be reversible. Ask: What would your life be like if you could only perform reversible actions? What would you need to give up? (For example, could you eat cooked food? Could you drive in gas-powered vehicles?) Have participants brainstorm their ideas and record them on sticky notes or index cards; show them where to post their ideas.



Discussion Extension for Ages 9+

6. Remind participants that quantum computers aren't performing actions like cooking food or cracking open eggs. They are doing mathematical operations. Ask: What are mathematical operations? [*Addition, subtraction, multiplication, division.*]
7. Ask: What do you think it means for a mathematical operation to be reversed? Facilitate a discussion and clarify that it means that you have enough information to get back the original numbers you started with, called inputs. For example, if you add 12 and 7 and get the result 19, what information do you need to get back the inputs?
 - If you only know the result (19) and the operation (addition), can you get back the inputs? [*No.*]
 - What other information do you need to know to get back the inputs? [*You need to know one of the inputs.*]
 - Let's think about another example: incrementing, or adding by 1. If you know that you incremented 5 times and the result was 17, can you get back the original input? [*Yes. It is 12.*]
8. Facilitate a discussion of this question: What do you need to know to make a mathematical operation reversible? [*You need to know the result, the operation, and at least one of the inputs.*]
9. Tell participants that quantum computers can perform operations on many numbers in very little time, the constraint of reversible operations means that it needs to save extra information so that it can reverse the operations, which takes up space. That extra information is stored in *ancilla bits*.



Connections to Standards

Next Generation Science Standards*

Crosscutting Concept: Patterns, Cause and Effect

NGSS Science and Engineering Practices: Using Mathematics and Computational Thinking, Constructing Explanations, Engaging in Argument from Evidence

Acknowledgements

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Reversibility with Paper

Cut or tear the paper in half.

Fold the paper in half.

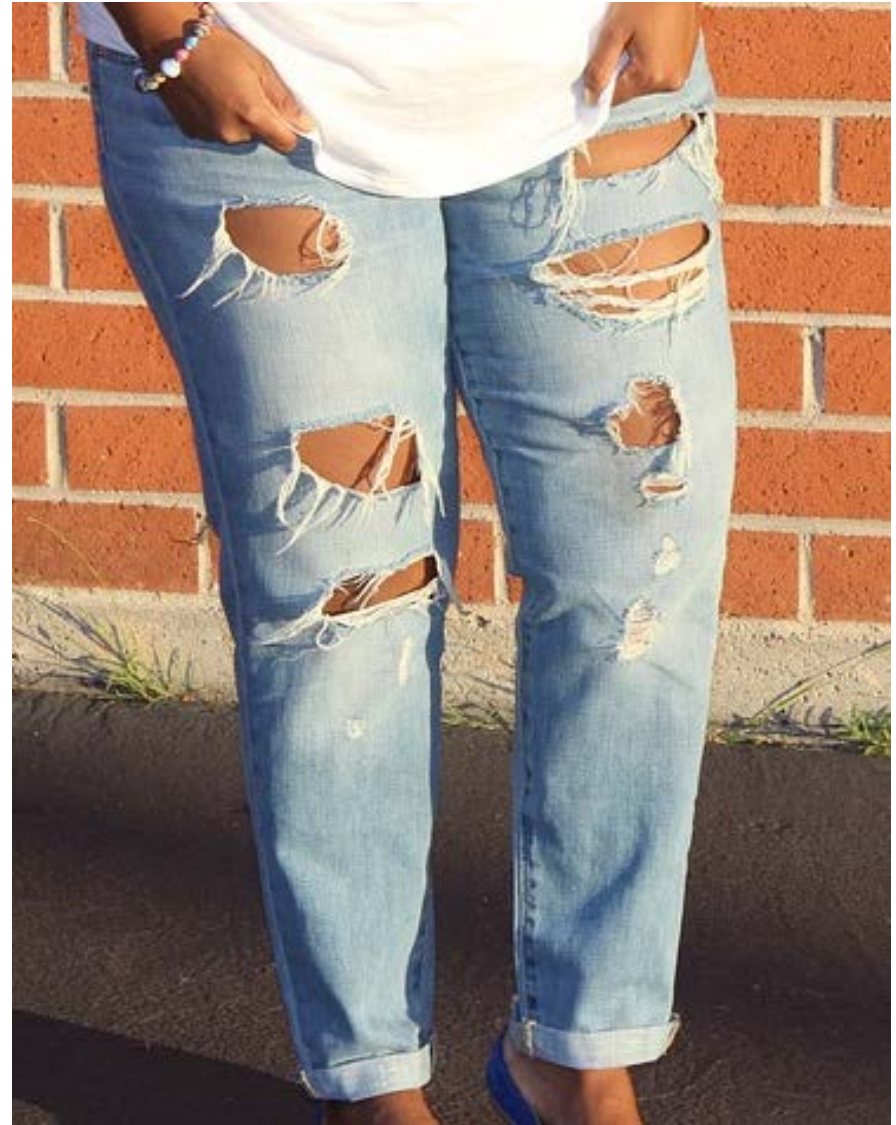
Cut or tear the paper.

Make a paper airplane.

New jeans



Ripped jeans



Savaman from Sao Paulo City / Ipiranga, Brasil [CC BY 2.0 (<https://creativecommons.org/licenses/by/2.0>)]

[Samantha Sophia](#) on [Unsplash](#)

Colored paper



Liz Lehman

Scissors cutting paper



Liz Lehman

Unfolded paper



Ulrike Mai on <https://pixabay.com>

Paper folded into a crane



<https://www.nicepik.com/>

Eggs in a carton



congerdesign on <https://pixabay.com>

Cracked egg



CraftyPease on <https://pixabay.com>

Closed plastic eggs



<https://www.nicepik.com/>

Open plastic eggs



Circe Denyer, <https://www.publicdomainpictures.net>

Bread



Marco Verch, [Flickr](#), [CC BY 2.0
(<https://creativecommons.org/licenses/by/2.0>)]

Toast



"[Toast!](#)" by [John McClumpha](#) is licensed under [Creative Commons Attribution 2.0](#)

Glass of water



<https://www.rawpixel.com>

Glass of tea



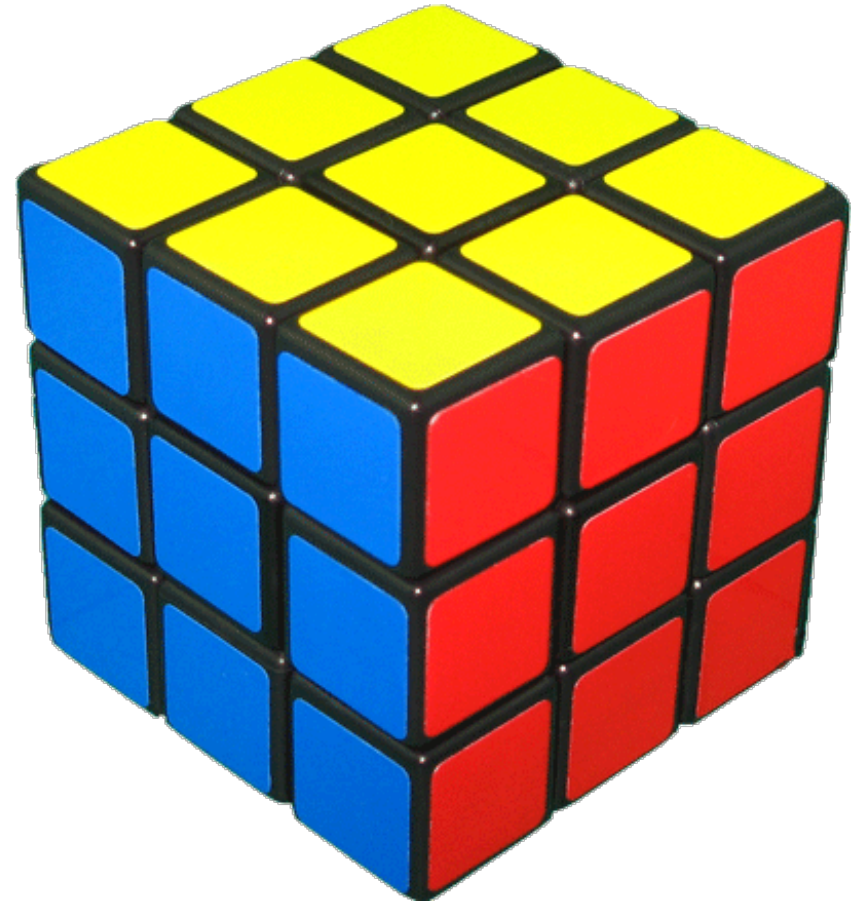
<https://pxhere.com>

Unsolved Rubik's Cube



<http://pngimg.com/> [CC BY-NC 4.0]
(<https://creativecommons.org/licenses/by-nc/4.0/>)

Solved Rubik's Cube



<http://www.pngall.com> [CC BY-NC 4.0]
(<https://creativecommons.org/licenses/by-nc/4.0/>)

Inflated balloon



K Whiteford (publicdomainpictures.net)

Popped balloon



Andrew Magill, [Flickr](https://www.flickr.com/photos/andrewmagill/), [CC BY 2.0
(<https://creativecommons.org/licenses/by/2.0/>)]

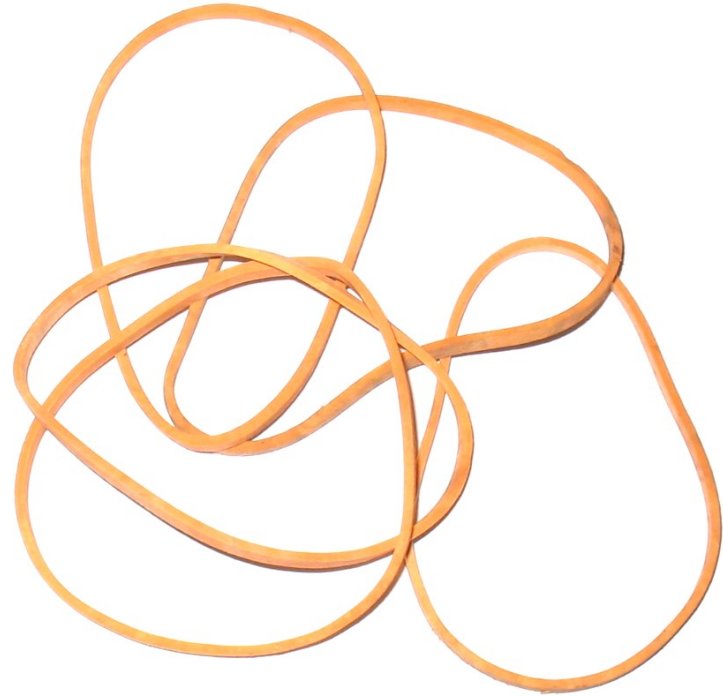
Puzzle pieces



Solved puzzle



Rubber band



Stretched rubber band



Balls of yarn



Skeeze on <https://pixabay.com>

Knitted mittens



Ugglemamma on <https://pixabay.com>

Uninflated balloons



Charles Rondeau (publicdomainpictures.net)

Inflated balloons



<https://www.rawpixel.com>

Zipped zipper



Liz Lehman

Unzipped zipper



Liz Lehman

Ice cube tray filled with water



Liz Lehman

Ice cube tray with ice



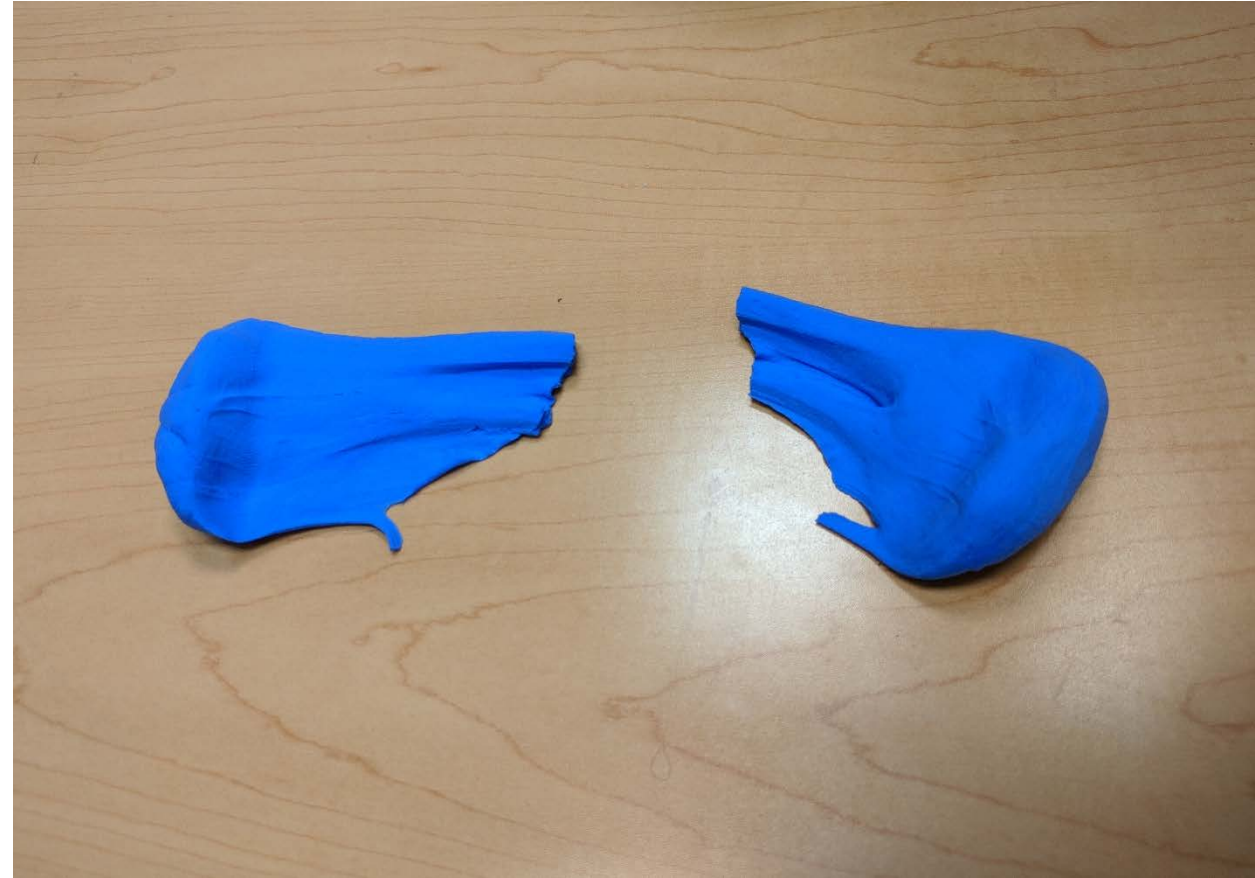
Liz Lehman

Clump of play dough



Liz Lehman

Clump of play dough in 2 pieces



Liz Lehman

Uncolored coloring page



Liz Lehman

Colored coloring page



Liz Lehman

I am in grade _____



Reversible or Not?

Draw or describe an action or change.

I think this action or change is reversible NOT reversible

I think this because _____

Ask a friend what they think!


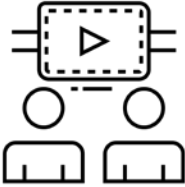










I think the action or change is reversible because _____

I think the action or change is NOT reversible because _____

I'm not sure because _____

Is It Reversible?

Consider each of the actions described below.
 Circle the actions that you think are reversible.
 Cross out the actions that you think are not reversible.
 It's OK if you're not sure!

<p>Building a tower of blocks</p> 	<p>Watching a movie</p> 	<p>Jumping in a puddle</p> 	<p>Climbing a ladder</p> 
<p>Painting a picture</p> 	<p>Taking a photograph</p> 	<p>Baking a pie</p> 	<p>Turning on a lamp</p> 
<p>Braiding hair</p> 	<p>Pouring water into a cup</p> 	<p>Letting the cat out of the bag</p> 	<p>Making a popsicle</p> 

Pick one action and explain your thinking about it. How did you decide if the action was reversible or not?

I am in grade _____




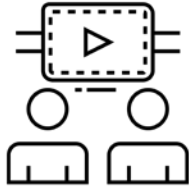










Is It Reversible?

Consider each of the actions described below. Mark if you think it is reversible or not, then explain your thinking. It's OK if you're not sure!

Action	Is it reversible?	Explain your thinking.
Building a tower of blocks	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Watching a movie	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Jumping in a puddle	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Climbing a ladder	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Painting a picture	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Taking a photograph	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Baking a pie	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Turning on a lamp	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Braiding hair	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Pouring water into a cup	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Letting the cat out of the bag	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	
Making a popsicle	<input type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	

Is It Reversible?

Consider each of the actions described below.
 Circle the actions that you think are reversible.
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 It's OK if you're not sure!

<p>Building a tower of blocks</p> 	<p>Watching a movie</p> 	<p>Jumping in a puddle</p> 	<p>Climbing a ladder</p> 
<p>Painting a picture</p> 	<p>Taking a photograph</p> 	<p>Baking a pie</p> 	<p>Turning on a lamp</p> 
<p>Braiding hair</p> 	<p>Pouring water into a cup</p> 	<p>Letting the cat out of the bag</p> 	<p>Making a popsicle</p> 

Explain your thinking. How did you decide if an action was reversible or not?

Answers will vary, but look for explanations that include the idea that reversible actions can be undone, such that the elements return to their initial states or the way they were before the action was performed.

Expect variation in the level of reversal that is considered acceptable. For example, some may consider "Making a popsicle" reversible because you can melt it but others may consider it not reversible because it's difficult to get back the original, separate ingredients.

I am in grade _____



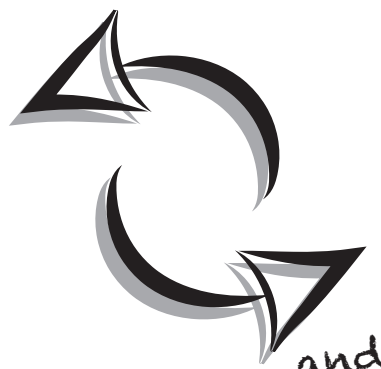
Is It Reversible?

Consider each of the actions described below. Mark if you think it is reversible or not, then explain your thinking. It's OK if you're not sure!

Action	Is it reversible?	Explain your thinking.
Building a tower of blocks	<input checked="" type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	You can dismantle the tower.
Watching a movie	<input type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You will remember it, even if you rewind the movie.
Jumping in a puddle	<input checked="" type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can jump back out. You can't get all the water back into the puddle.
Climbing a ladder	<input checked="" type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	You can climb back down.
Painting a picture	<input type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can't get all the paint off the canvas.
Taking a photograph	<input checked="" type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can delete a digital photo. You can't un-do taking a film photo.
Baking a pie	<input type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can't un-bake the pie.
Turning on a lamp	<input checked="" type="checkbox"/> Reversible <input type="checkbox"/> Not reversible	You can turn it back off.
Braiding hair	<input checked="" type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can unbraid it. You can't make hair exactly the same as it was before.
Pouring water into a cup	<input checked="" type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can pour the water back. You can't get it all back in.
Letting the cat out of the bag	<input type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	It might not want to go back. The other person can't un-learn your secret.
Making a popsicle	<input checked="" type="checkbox"/> Reversible <input checked="" type="checkbox"/> Not reversible	You can unfreeze it. You can't get back to the original ingredients.

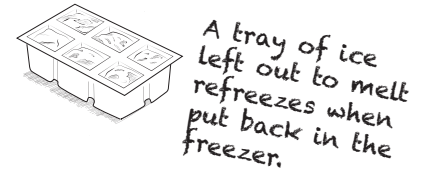
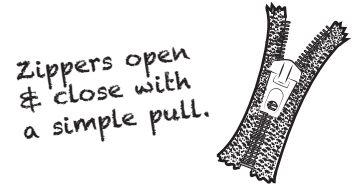
A PEEK INTO...

Quantum

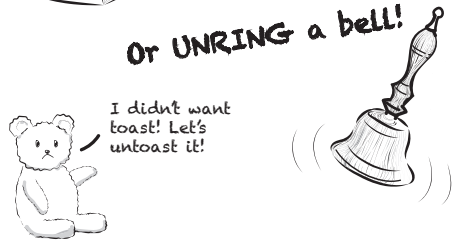
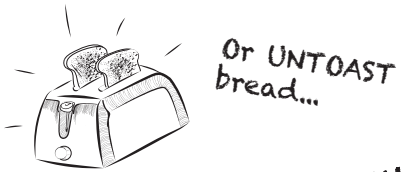


and Reversibility

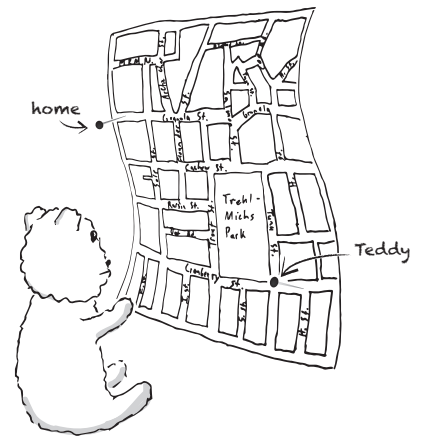
Reversibility is all around us!



Some things are NOT reversible

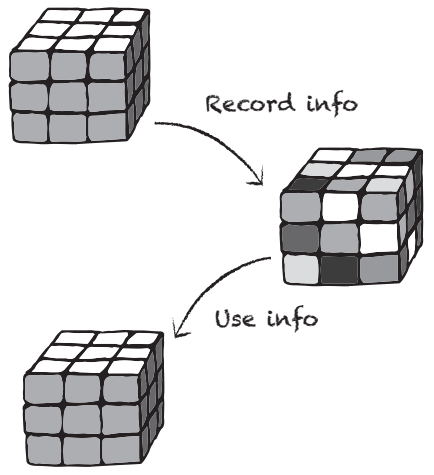


Reversing may require recording information



Without a map, what information does Teddy need to get back home by the same route?

Let's solve a Rubik's Cube!



What information would you record to help unscramble your Rubik's Cube?

Is addition reversible??

If I added two numbers and got 8...

$$? + ? = 8$$

...can you tell me what those numbers were?

- 1 + 7 = 8
- 2 + 6 = 8
- 3 + 5 = 8
- 4 + 4 = 8

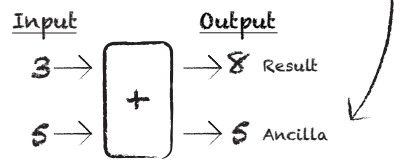


Addition is NOT reversible!

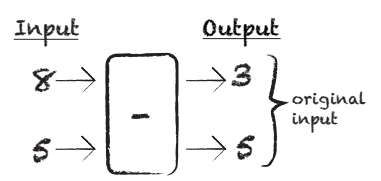
In programs, you know the order of operations and result but not the starting value

Reversibility in Quantum Computing

Quantum computers store extra information in ancilla bits so they can reverse operations.



With this extra information, we can use subtraction to get the original input!

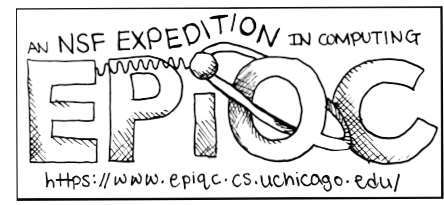


For more Quantum Computing Zines visit:

<https://www.epiqc.cs.uchicago.edu/resources/>

August 2019

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Share what you've learned about reversibility!

- Teach someone else about what it means for an action to be reversible.
- Identify reversible and irreversible actions during your daily activities.
- Create a Reversibility Obstacle Course: The leader directs actions for the other players to complete. After they have completed them, they have to reverse them to return to where they started. For example, the leader might say, "Hop forward 3 times, then run to the swings, then sit in a swing." After completing those actions, the players would then have to get up from the swing, run backwards, and hop backwards.

Start with three actions, then increase the number. Try to figure out how many actions can the players remember to do in reverse.

Be prepared to discuss the rules. For example, do the players need to perform the actions in reverse order?

- Play a game of Reversible Simon Says: The person playing Simon says actions for the other players to perform. The other players should only perform the actions stated by Simon if they are reversible. For example, Simon might say, "Take one step to the right." The other players should perform this action because it can be reversed by taking one step to the left.

Be prepared to discuss if the actions are reversible or not.

- Play Reversible Hopscotch: Start with 2 players on opposite ends of a hopscotch court. The first player hops across the course in any manner they choose. The second player has to correctly reverse the path. The players then alternate roles.